

Junior Balkan MO 2001

Nicosia, Cyprus

- [1] Solve the equation $a^3 + b^3 + c^3 = 2001$ in positive integers.

Mircea Becheanu, Romania

- [2] Let ABC be a triangle with $\angle C = 90^\circ$ and $CA \neq CB$. Let CH be an altitude and CL be an interior angle bisector. Show that for $X \neq C$ on the line CL , we have $\angle XAC \neq \angle XBC$. Also show that for $Y \neq C$ on the line CH we have $\angle YAC \neq \angle YBC$.

Bulgaria

- [3] Let ABC be an equilateral triangle and D, E points on the sides $[AB]$ and $[AC]$ respectively. If DF, EF (with $F \in AE, G \in AD$) are the interior angle bisectors of the angles of the triangle ADE , prove that the sum of the areas of the triangles DEF and DEG is at most equal with the area of the triangle ABC . When does the equality hold?

Greece

- [4] Let N be a convex polygon with 1415 vertices and perimeter 2001. Prove that we can find 3 vertices of N which form a triangle of area smaller than 1.